Chapter 23
Electric Potential

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• Electric Potential Due to Point Charges
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Units of Chapter 23
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• Determination of Capacitance
• Capacitors in Series and Parallel
• Electric Energy Storage
• Dielectrics
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Electrostatic Potential Energy and Potential Difference

The electrostatic force is conservative – potential energy can be defined

Change in electric potential energy is negative of work done by electric force:

\[ U_b - U_a = -qEd \]

Electric potential is defined as potential energy per unit charge:

\[ V_e = \frac{U}{q} \]

Unit of electric potential: the volt (V).

1 V = 1 J/C.
Electrostatic Potential Energy and Potential Difference

Only changes in potential can be measured, allowing free assignment of \( V = 0 \).

\[ V_{ba} = V_b - V_a = \frac{U_b - U_a}{q} = \frac{W_{ba}}{q} \]

Electrostatic Potential Energy and Potential Difference

Analogy between gravitational and electrical potential energy:

Relation between Electric Potential and Electric Field

Work is charge multiplied by potential:

\[ W = -q(V_b - V_a) = -qV_{ba} \]

Work is also force multiplied by distance:

\[ W = Fd = qEd \]
Relation between Electric Potential and Electric Field

The difference in potential energy between any two points in space is given by

\[ U_{b} = U_{a} - \int_{a}^{b} E \cdot dl \]

Substituting \( F \):

\[ V_{b} = V_{a} - \int_{a}^{b} E \cdot dl \]

*Relation between Electric Potential and Electric Field

Solving for the field,

\[ E = - \frac{V_{b} - V_{a}}{d} \]

If the field is not uniform, it can be calculated at multiple points:

\[ E_{x} = - \frac{\Delta V}{\Delta x} \]
### Equipotential Lines

An equipotential is a line or surface over which the potential is constant.

Electric field lines are perpendicular to equipotentials.

The surface of a conductor is an equipotential.

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### The Electron Volt, a Unit of Energy

One electron volt (eV) is the energy gained by an electron moving through a potential difference of one volt.

\[ 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J} \]
Electric Potential Due to Point Charges

The electric potential due to a point charge can be derived using calculus.

\[ V = k \frac{Q}{r} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \]

These plots show the potential due to (a) positive and (b) negative charge.

Using potentials instead of fields can make solving problems much easier – potential is a scalar quantity, whereas the field is a vector.
The potential due to an electric dipole is just the sum of the potentials due to each charge, and can be calculated exactly.

Approximation for potential far from dipole:

\[ V \approx \frac{kQl \cos \theta}{r^2} \]

Or, defining the dipole moment \( p = Ql \),

\[ V \approx \frac{kp \cos \theta}{r^2} \]
Chapter 24
Capacitance, Dielectrics, Electric Energy Storage

Capacitance
A capacitor consists of two conductors that are close but not touching. A capacitor has the ability to store electric charge.

Capacitance
Parallel-plate capacitor connected to battery. (b) is a circuit diagram.
Capacitance

When a capacitor is connected to a battery, the charge on its plates is proportional to the voltage:

\[ Q = CV \]

The quantity \( C \) is called the capacitance.

Unit of capacitance: the farad (F)

\[ 1 \text{ F} = 1 \text{ C/V} \]

Capacitance

The capacitance does not depend on the voltage; it is a function of the geometry and materials of the capacitor.

For a parallel-plate capacitor:

\[ C = \varepsilon_0 \frac{A}{d} \]

Dielectrics

A dielectric is an insulator, and is characterized by a dielectric constant \( K \).

Capacitance of a parallel-plate capacitor filled with dielectric:

\[ C = K\varepsilon_0 \frac{A}{d} \]
Dielectrics

Dielectric strength is the maximum field a dielectric can experience without breaking down.

<table>
<thead>
<tr>
<th>Material</th>
<th>Dielectric constant $K$</th>
<th>Dielectric strength $(V/m)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vacuum</td>
<td>1.0000</td>
<td></td>
</tr>
<tr>
<td>Air (Lair)</td>
<td>1.0000 $\times 10^6$</td>
<td></td>
</tr>
<tr>
<td>Paraffin</td>
<td>2.2 $\times 10^6$</td>
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<tr>
<td>Polyethylene</td>
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</tr>
<tr>
<td>Polypropylene</td>
<td>4.4 $\times 10^6$</td>
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<tr>
<td>Paper</td>
<td>5.7 $\times 10^6$</td>
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</tr>
<tr>
<td>Quartz</td>
<td>8.3 $\times 10^6$</td>
<td></td>
</tr>
<tr>
<td>Oil</td>
<td>4 $\times 12^6$</td>
<td></td>
</tr>
<tr>
<td>Glass, Pyrex</td>
<td>5 $\times 10^6$</td>
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</tr>
<tr>
<td>Rubber</td>
<td>6.7 $\times 10^6$</td>
<td></td>
</tr>
<tr>
<td>Porcelain</td>
<td>6.8 $\times 10^6$</td>
<td></td>
</tr>
<tr>
<td>Mica</td>
<td>7 $\times 150^6$</td>
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<tr>
<td>Water (liquid)</td>
<td>80</td>
<td></td>
</tr>
<tr>
<td>Nitrocellulose</td>
<td>300</td>
<td>$8 \times 10^6$</td>
</tr>
</tbody>
</table>

Molecular Description of Dielectrics

The molecules in a dielectric tend to become oriented in a way that reduces the external field.

This means that the electric field within the dielectric is less than it would be in air, allowing more charge to be stored for the same potential.
Electric Energy Storage

A charged capacitor stores electric energy; the energy stored is equal to the work done to charge the capacitor.

\[ PE = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C} \]

Electric Energy Storage

The energy density, defined as the energy per unit volume, is the same no matter the origin of the electric field:

\[ \text{energy density} = \frac{PE}{\text{volume}} = \frac{1}{2} \varepsilon_0 E^2 \]

The sudden discharge of electric energy can be harmful or fatal. Capacitors can retain their charge indefinitely even when disconnected from a voltage source – be careful!

17.9 Storage of Electric Energy

Heart defibrillators use electric discharge to "jump-start" the heart, and can save lives.
A cathode ray tube contains a wire cathode that, when heated, emits electrons. A voltage source causes the electrons to travel to the anode.

The electrons can be steered using electric or magnetic fields.

Television and computer monitors (except for LCD and plasma models) have a large cathode ray tube as their display. Variations in the field steer the electrons on their way to the screen.
17.10 Cathode Ray Tube: TV and Computer Monitors, Oscilloscope

An oscilloscope displays an electrical signal on a screen, using it to deflect the beam vertically while it sweeps horizontally.

17.11 The Electrocardiogram (ECG or EKG)

The electrocardiogram detects heart defects by measuring changes in potential on the surface of the heart.

Summary of Chapter 17

- Electric potential energy:
  \[ \text{PE}_b - \text{PE}_a = -qEd \]

- Electric potential difference: work done to move charge from one point to another

- Relationship between potential difference and field:
  \[ E = \frac{-V_{ba}}{d} \]
Summary of Chapter 17

- Equipotential: line or surface along which potential is the same
- Electric potential of a point charge:
  \[ V = k \frac{Q}{r} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \]
- Electric dipole potential:
  \[ V \approx k d \cos \theta \frac{1}{r^2} \]

Summary of Chapter 17

- Capacitor: nontouching conductors carrying equal and opposite charge
- Capacitance:
  \[ Q = CV \]
- Capacitance of a parallel-plate capacitor:
  \[ C = \epsilon_0 \frac{A}{d} \]

Summary of Chapter 17

- A dielectric is an insulator
- Dielectric constant gives ratio of total field to external field
- Energy density in electric field:
  \[ \text{energy density} = \frac{\text{PE}}{\text{volume}} = \frac{1}{2} \epsilon_0 E^2 \]