

Equations to Know

**Chapter 30**

Mutual Inductance

$$M_{21} = \frac{N_2 \Phi_{21}}{I_1}$$

EMF Induced in Coil 2 Due to a Changing Current in Coil 1 (2 parts)

$$\mathcal{E}_2 = -N \frac{d\Phi_{21}}{dt} = -M \frac{dI_1}{dt}$$

Mutual Inductance for a Coil Wrapped around a Solenoid

$$M_{CS} = \mu_0 \left( \frac{NA}{\ell} \right)_S N_C$$

Self-Inductance

$$L = \frac{N\Phi_B}{I}$$

EMF Due to Self-Inductance (2 parts)

$$\mathcal{E} = -N \frac{d\Phi_B}{dt} = -L \frac{dI}{dt}$$

Power being supplied to an Inductor

$$P = LI \frac{dI}{dt}$$

Energy Stored in an Inductor

$$U = \frac{1}{2} LI^2$$

Energy Stored in a Solenoid

$$U = \frac{1}{2} \frac{B^2}{\mu_0} A\ell$$

Energy Density in a Magnetic Field (2 parts)

$$u = \frac{U}{Volume} = \frac{1}{2} \frac{B^2}{\mu_0}$$

Coaxial Cable Inductance per Unit Length with Picture

$$\frac{L}{\ell} = \frac{\mu_0}{2\pi} \ln \frac{r_2}{r_1}$$

Energy Stored per Unit Length in a Coaxial Cable

$$\frac{U}{\ell} = \frac{\mu_0 I^2}{4\pi} \ln \frac{r_2}{r_1}$$

LR Circuit: Time Constant

$$\tau = \frac{L}{R}$$

LR Circuit: Current @ t=0 when battery is connected

$$I = \frac{V_0}{R} \left( 1 - e^{-\frac{Rt}{L}} \right)$$

LR Circuit: Current @ t=0 when circuit is “shorted”

$$I = I_0 e^{-\frac{Rt}{L}}$$

LC Circuit: Angular Frequency (2 parts)

$$\omega = 2\pi f = \sqrt{\frac{1}{LC}}$$

*LC* Circuit: Current

$$I = \underbrace{\omega Q_0}_{I_0} \sin(\omega t + \phi)$$

*LC* Circuit: Total Energy Stored (2 parts)

$$U = U_E + U_B = \frac{1}{2} \frac{Q_0^2}{C}$$

*LRC* Circuit: Time Constant (2 parts)

$$\tau = \frac{1}{\alpha} = \frac{2L}{R}$$

*LRC* Circuit: Angular Frequency

$$\omega' = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

*LRC* Circuit: Charge across Capacitor

$$Q = Q_0 e^{-\frac{R}{2L}t} \cos(\omega' t + \phi)$$

*LRC* Circuit: Underdamped

$$R^2 < \frac{4L}{C}$$

*LRC* Circuit: Critically Damped

$$R^2 = \frac{4L}{C}$$

*LRC* Circuit: Overdamped

$$R^2 > \frac{4L}{C}$$